Formal Methods at Work

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Part I

Where Do We Stand?



Today's car: typically 100 processing units, 100 M. lines of code, 600 *Quijotes*, 7.000 programmer years.





Plane: computers manage controls, calculate routes, \dots





Large interconnected systems: independent, isolated, automatic decision making, which must be globally correct.





- Cell phones (from O.S. to compression algorithms to user interfaces).
- HDTV (routing, encoding and decoding).
- Buy and sell on the Internet (web interfaces, databases, encryption).
- Stock market (algorithmic trading, high frequency trading).





- Managed by extremely complex software.
- / All of them critical to a certain degree.
- / Some **extremely** critical





- $\sqrt{}$ Managed by extremely complex software.
- $\sqrt{\ }$ All of them *critical* to a certain degree.
 - / Some **extremely** critical

Challenge:

How to develop complex software, with resources that are always limited, assuring that it will work correctly?



(Only showing some types of problems)

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July 16, 2012: Skype bug sends messages to unintended recipients.

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The Ariane 5 Incident

Example: effect of a single integer overflow.





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From the outside...

- June 4, 1996: After launch, the Ariane 5 rocked exploded.
- This was its maiden voyage.
- It flew for about 37 sec. only in Kourou's sky.
- No injury in the disaster.



Mechanical details

- Normal behavior of the launcher for 36 sec. after lift-off.
- Failure of both Inertial Reference Systems almost simultaneously.
- Strong pivoting of the nozzles of the boosters and Vulcain engine.
- Self-destruction at an altitude of 4000 m. (1000 m. from the pad).



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Forensic analysis

- Both inertial computers failed because of overflow on one variable.
- This caused a software exception and stops these computers.
- These computers sent post-mortem info through the bus.
- Normally the main computer receives velocity info through the bus.
- The main computer was confused and pivoted the nozzles.



But, why?

- The faulty program was working correctly on Ariane 4.
- The faulty program was not tested for A5 (since it worked for A4).
- But the velocity of Ariane 5 is far greater than that of Ariane 4.
- That caused the overflow in one variable.
- The faulty program happened to be useless for Ariane 5.



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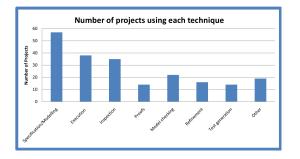
Message

- Does the product conform to specifications?
- Maybe it's important to carry experience in formal methods to industry!
- Is it done?



Formal Methods in Industry

- Actually, yes at least in some domains, for some types of applications.
- Using many approaches, actually [WLBF09].



We will see some examples







- Only two buttons: start and stop.
 - No crossroads, no people crossing, . . .
- Should be easy to automate!
- But...
 - Wait for people to get on board.



¹Same with trains, only worse.



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 - How can you to try to see if it works?¹



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 - And, if it doesn't, how long does it take to reproduce the bug in your computer?



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 - How can you to try to see if it works?¹
 - And, if it doesn't, how long does it take to reproduce the bug in your computer?
 - Or, plainly, how can you reproduce it?



¹Same with trains, only worse.



Towards an Automatically Managed Subway Line

- Add extra sensors.
- Add extra mechanisms (doors apart apart from coaches').
- Model the environment very precisely.
- Correctness by Construction.



Paris Metro Line 14

- October 15th, 1998, Tolbiac to Madeleine. (Now extended)
- 40000 passenger / hour, 85 sec. between trains in peak hour.
- 2009: 60 million passengers / year.
- Decision based on previous experience:
 - Completely automated line.
 - Completely developed using formal methods for control systems.
 - Having manually and automatially driven trains.





Subsystems

- Automatic control and signaling.
- Platform doors.
- Audio and Video.
- Operating control center.



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Subsystems

- Automatic control and signaling.
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- Running alone on specific, non-interruptible, microprocessor boards.
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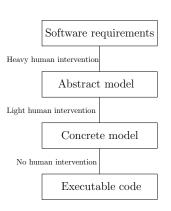
Subsystems

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- In the train.
- In the operating control center.
- Along the tracks.
- Running alone on specific, non-interruptible, microprocessor boards.
- Platform doors.
- Audio and Video.
- Operating control center.
- Developed using the B Method [Abr96], now evolved into Event B [Abr10].



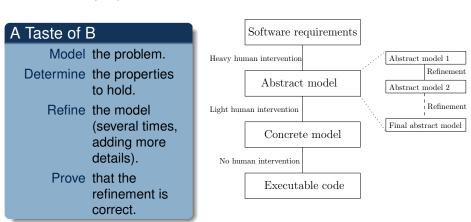
Make sure that every step is correct

A Taste of B Model the problem. Determine the properties to hold. Refine the model (several times, adding more details). Prove that the refinement is correct.



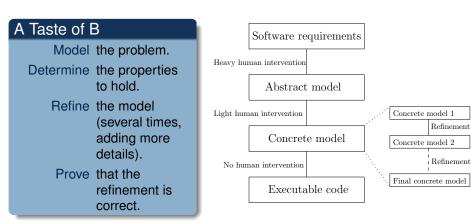


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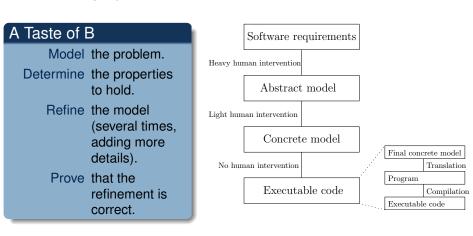


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Make sure that every step is correct





```
INVARIANTS
      invBDay: birthday \in PERSON \rightarrow DATE
EVENTS
Initialisation
    begin
         initBDay : birthday := \emptyset
    end
Event addBDay ≘
    any
        p, d
    where
         inPerson : p \in PERSON
         {\tt inDate} : d \in DATE
    then
         newBDay : birthday(p) := d
    end
END
```



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    where
          inPerson : p \in PERSON
          {\tt inDate} : d \in DATE
          \texttt{checkBday}: p \not\in dom(birthday)
    then
          newBDay : birthday(p) := d
    end
END
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Proofs: Prove **mathematically** refinements are right.



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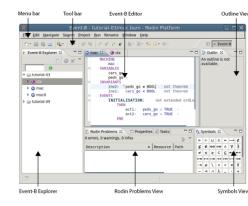
Note: invariants are the most important piece of information. Although many proofs are not aimed at establishing invariants, virtuall all of them involve invariants.

```
\begin{array}{l} \textbf{a}, \textbf{c} \in \mathbb{N}, a+b+c = n, n > 0 \lor n < d, \neg(\textbf{c} > \textbf{0}) \vdash (a+b < d \land c = \\ \textbf{0}) \lor a > 0 \lor (b > 0 \land a = 0) \\ \textbf{a}, \textbf{c} \in \mathbb{N}, a+b+c = n, n > 0 \lor n < d \vdash (a+b < d \land c = 0) \lor \textbf{c} > \textbf{0} \lor a > \\ \textbf{0} \lor (b > 0 \land a = 0) \\ \textbf{a}, \textbf{b}, \textbf{c}, \textbf{d}, n \in \mathbb{N}, 0 < d, n \leq d, a+b+c = n, a = 0 \lor c = \\ \textbf{0}, \textbf{0} < \textbf{n} \lor \textbf{n} < d \vdash (a+b < d \land c = 0) \lor c > 0 \lor a > 0 \lor (b > 0 \land a = 0) \end{array}
```



Tools!

- Automate some (many) proofs.
- Automatically generate code.
- Many advantages when code is generated.
- Example at hand: code duplication.
 - Electronic in tunnels: interference with boards.
 - Possible corruption of data.
 - All data duplicated in different formats.
 - Code works on both copies.
 - Constant comparison for consistency.





Statistics

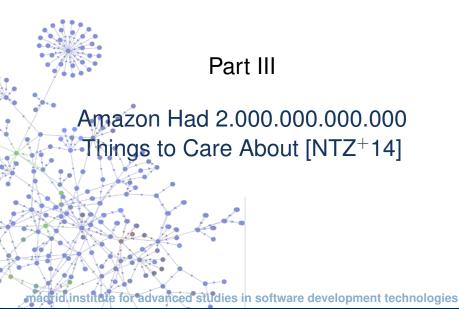
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- Time to develop: 4 years (aprox.)



Statistics

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- Lines of Ada: 86.000 .
- Lemmas of B: 27.800 .
- Automatically proven: 92%.
- Time to develop: 4 years (aprox.)
- Bugs in development computer: 0
- Bugs in target computer: 0
- Bugs in on-site tests: 0
- Bugs since deployment: 0







Landscape

Some numbers for AWS's S3

- 2013: 2.000.000.000.000 (2 trillions) objects, 1.1 million requests per second.
- High availability.
- Scalability.
- S3 just one AWS service.
- Essential complexity high \rightarrow unavoidable human errors.



Previously in...

- Standard "verification" techniques in industry.
 - Deep design reviews.
 - Code reviews (c.f. DB train code reviews).
 - Static code analysis.
 - Stress testing.
 - Fault-injection testing.
 - ...

... human intuition is poor at estimating the true probability of supposedly "extremely rare" combinations of events in systems operating at a scale of millions of requests per second.



The History According to the Starring Roles

- Engineer C.N. dissatisfied with bugs in implementations of distributed algorithms.
- Looked for ways to correct them not thinking on formal methods.
- But read paper on formal verification of Chord using Alloy.
- Tried to use it, but not rich enough no good for formal methods!



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- But read paper on formal verification of Chord using Alloy.
- Tried to use it, but not rich enough no good for formal methods!
- C.N. read a paper on Leslie Lamport Paxos algorithm essential in distributed systems.
- At the end of the paper, a TLA+ [Lam02] / TLC formalization.
- TLA+ also devised by Leslie Lamport.
- Maybe TLA+ / TLC was worth something?
- Tried the same example as in Alloy success!



The Busy Engineers

- But engineers too busy to try new things.
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Enter DynamoDB

- Scalable, high-performance, high-availability storage.
- Testing, stressing, fault injection but really high confidence was necessary.
 - Otherwise data from companies could be lost.
- T.R. (DynamoDB's coauthor) went on to prove relevant properties.
- Informal proofs already found bugs.
- Which other subtle problems could be hidden?



TLA+ Time

- T.R. learned TLA+, formalized (some) DynamoDB algorithms.
- Run distributed version of model checker TLC.
 - Cluster of ten EC² instances.
 - Each 8 cores + hyperthreads.
 - 23 GB ram.
- Small part of algorithm OK.
- But in the full fault-tolerance algorithm a bug was found.
 - Very subtle many conditions had to be met.
 - But historically possible.
 - Bug had passed all reviews.
 - Other two bugs were found later on.



The History Goes On

- New DynamoDB features first modeled and verified in TLA+ and bugs were found ahead of time.
- Presentation to teams: Debugging Designs.
 - Exahustively testable pseudo-code.
- New fault-tolerant distributed algorithm specified and checked.
 - Two bugs found.
- Management started pushing TLA+ usage in teams.



What the Protagonists Say...

[...] help engineers to get the design right. [...] If the design is broken then the code is almost certainly broken. Coding mistakes extremely unlikely to compensate mistakes in design.

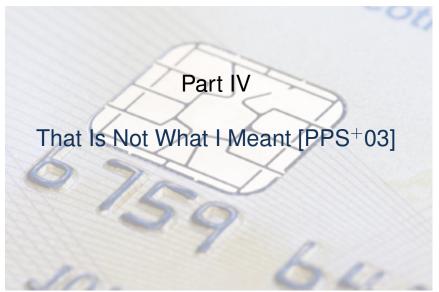
Engineers probably deceived into believing that code is 'correct' because appears to correctly implement the broken design. Unlikely to realize that design is incorrect while focusing on coding.

[...] gain a better understanding of the design. [...] can only increase chances that they will get code right.

[...] write better assertions [...], a good way to reduce errors in code.

Formal methods help engineers to find strong invariants, so formal methods can help to improve assertions, which help improve the quality of code.







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- Natural language is ambiguous.
- Even if it's not, it relies a lot on "common knowledge" or "situational knowledge".
- Kids give us lots of examples: flawless reasoning without knowledge.



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- Do not leave the water running. What will happen if we run out of water?
- We buy another faucet.
- (Pointing below the sink). Look: the tap gets water from the pipe, which comes from the wall. Buying another faucet will not help. Now, what would be do?



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- We buy another wall.

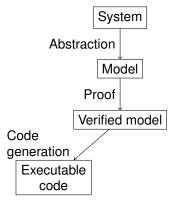


A Different Experiment

- Existing, well-proven implementation of a smartcard.
- Natural language specification.
- How well can a team of engineers capture understand these specifications?

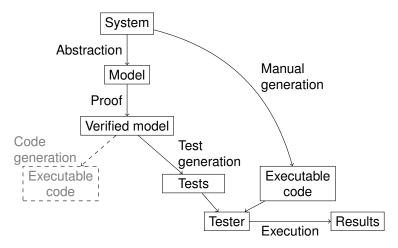


Using Models to Generate Tests





Using Models to Generate Tests





A SmartCard is...

- Fully programmable one-chip computer.
- Microprocessor, RAM (currently 256-4096 Bytes), EEPROM (2-16 KBytes), and ROM (8-64 KBytes).
- Hierarchical filesystem.
- Serial interface.
- Sometimes specialized cryptographic microprocessor.



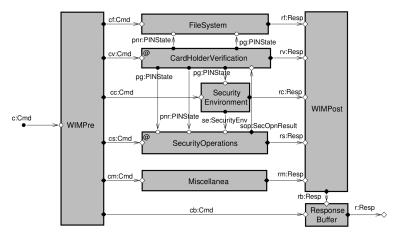
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- Hierarchical filesystem.
- Serial interface.
- Sometimes specialized cryptographic microprocessor.
- Command interpreter:
 - Read commands from stdin.
 - Interpret, execute, write output to stdout.
 - Execution usually depends on previous commands.



System Under Study

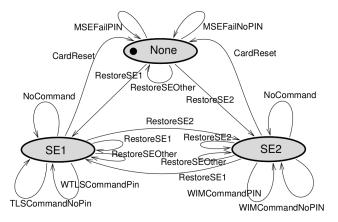
WAP module in GSM standard, implemented in a SmartCard.





Subcomponents

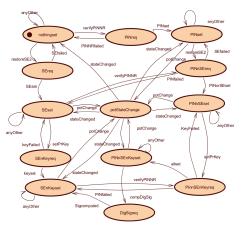
• Each subcomponent has a expected behavior (i.e., what it expects to receive and return in every state).



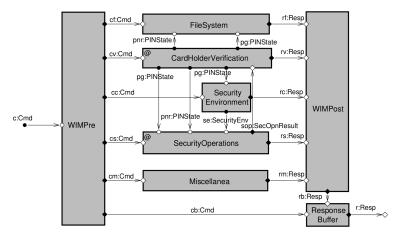


Tester: Behavior

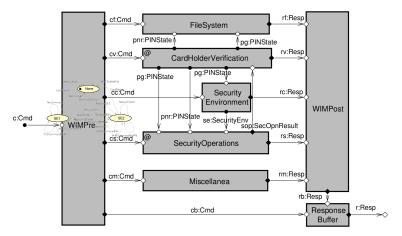
From the behavior of the component one can extract the expected behavior of the tester: what it has to do at every moment to check the component.



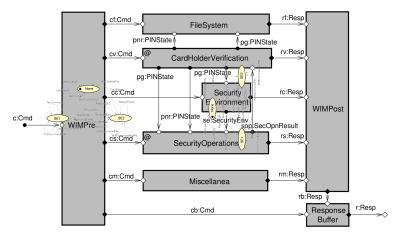




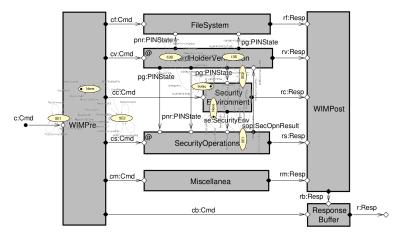




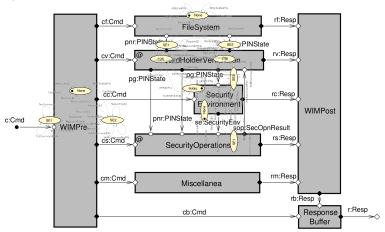




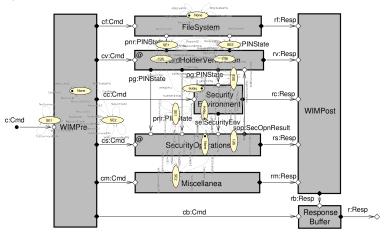




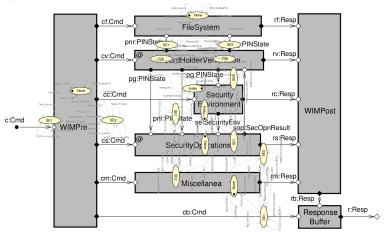




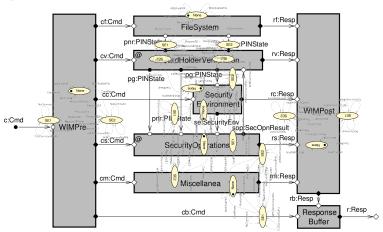














The Behavior of the Test Suite

Buffer



The Behavior of the Test Suite rf:Resp cf:Cmd wetem. pnr:PINState pg:PINState rv:Resp cv:Cmd pg:PINE cc:Umd Envir **WIMPost** se:Sec_rityEnv sop_S-cOpnReson c:Cmd WIM rs:Resp CS. Omi rm:Resp cm:Cmd rb:Resp r:Resp Response cb:Cmd



Test Coverage and Generation

- Testing cannot (in general) ensure correctness.
- Only existence of errors can be proven.
- Exhaustive testing: very expensive (in time to generate tests and to execute them)
- Test generation needs to execute the program.
 - If I call operation A with data D, which output would I obtain?



Test Generation for the SmartCard

- Using CLP.
- For a component a with a state machine, a collection of clauses like

```
step_a(StateIn, Input, StateOut, Output):-
    guard(StateIn, Input),
    assign(StateIn, Input, StateOut, Output).
```

• Different components can be chained togeter:

```
step_comp(StateIn, In, StateOut, Out):-
    step_a(StateOut, In, S0, O0),
    step_b(S0, O0, S1, O1),
    ...
    step_k(Sn, On, StateOut, Out).
```

- Enumerate traces.
- Use constraints to reduce trace sizes.



CLP to Reduce Traces

 Transition has to read value v from input channel i.

```
v = read(i);
if (v == k) then ...
else ...
```

- In else branch: assuming all possible values for v not feasible.
- Make a trace with v = k and another with $v \neq k$.
- ullet Constraint in the latter o generate refined feasible traces later on.
 - Requiring v = k after that $\rightarrow v \neq k \land v = k \rightarrow$ trace not generated.
 - A trace that requires $v \ge k$ is reduced to requiring v > k.
- Using sets of values (= constraints) helps reduce the search space.
- Still, some operations are difficult to model.
- AskRandom(n): only length modeled.



Evaluation

- 60.000 test sequences, varying length.
- Testing with only 2%-3% of sequences.
- Around one hour to execute.
- Summary: out of 1506 test sequences, 84 mistmatches.
- All of them due to misinterpretation of documentation or faults in recently optimized versions of software.



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- Around one hour to execute.
- Summary: out of 1506 test sequences, 84 mistmatches.
- All of them due to misinterpretation of documentation or faults in recently optimized versions of software.
- Make no assumptions.
- Premature optimization is the root of all evil.



Part V

What Now?



Conclusions

- Yes, formal methods are used in industry more than usually thought.
- Not to write payroll software.
 - But payroll software is already written...
- High-availability, dependable software.
 - NASA; Prolog to formalize JVM class system; SLAM at Microsoft; Esterel for hardware, avionics, and cars; Airbus; ... automotive industry, cyber-physical systems.
- Also to discover bugs in existing implementations.
 - E.g., FREAK SSL negotiation bug team INRIA, Microsoft Research, IMDEA Software Institute.



Recommendations [BH06] and Old Man Sayings

- Use well-tested, well-documented formal method.
- With tool support.
- If possible, have an expert at hand at least at the beginning.
- Document everything: every assumption, every decision.
- Don't lower quality standards.
- Test and test again.



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- Test and test again.
- Trying to formalize will force you to think about a problem. Thinking about a problem will make you understand it.



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Formal Methods at Work

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